

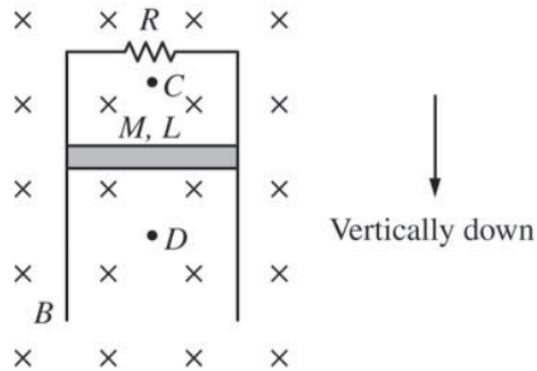
Instructions

This test is “open note” in that you are allowed to use your own notes and materials (the textbook) for developing your solutions to these problems. In solving, you may *not* use other sources (the Internet, friends, etc.) You may use a calculator and the AP Physics C *Table of Information and Equation Tables* in solving these problems. You will have 45 minutes to solve the two Free Response problems.

On separate sheets of blank paper (notebook paper, lab paper, printer paper), put your name at the top of every page, and write your answers for each part of the following two problems. Write your answers on only one side of a sheet, and place answers in numeric order on your paper even if you don't necessarily solve them in that order. Clearly identify what problem you are solving (“2.b” for example), show your work, and identify your final answer for each problem with a box around it. If you have written down work that you later want the grader to not evaluate, clearly cross out that work.

You will have 45 minutes to complete your solutions. When finished, scan your work and submit it to your teacher as instructed.

Free Response Questions (15 points each)



1. A conducting bar of mass M , length L , and negligible resistance is connected to two long vertical conducting rails of negligible resistance. The two rails are connected by a resistor of resistance R at the top. The entire apparatus is located in a magnetic field of magnitude B directed into the page, as shown in the figure above. The bar is released from rest and slides without friction down the rails.

(a) What is the direction of the current in the resistor? ___ Left ___ Right

(b)

i. Is the magnitude of the net magnetic field above the bar at point C greater than, less than, or equal to the magnitude of the net magnetic field before the bar is released?

___ Greater than ___ Less than ___ Equal to

Justify your answer.

ii. While the bar is above point D , is the magnitude of the net magnetic field at point D greater than, less than, or equal to the magnitude of the net magnetic field before the bar is released?

___ Greater than ___ Less than ___ Equal to

Justify your answer.

Express your answers to parts (c) and (d) in terms of M , L , R , B , and physical constants, as appropriate.

(c) Write, but do NOT solve, a differential equation that could be used to determine the velocity of the falling bar as a function of time t .

(d) Determine an expression for the terminal velocity v_T of the bar.

Express your answers to parts (e) and (f) in terms of v_T , M , L , R , B , and physical constants, as appropriate.

(e) Derive an expression for the power dissipated in the resistor when the bar is falling at terminal velocity.

(f) Using your differential equation from part (c), derive an expression for the speed of the falling bar $v(t)$ as a function of time t .

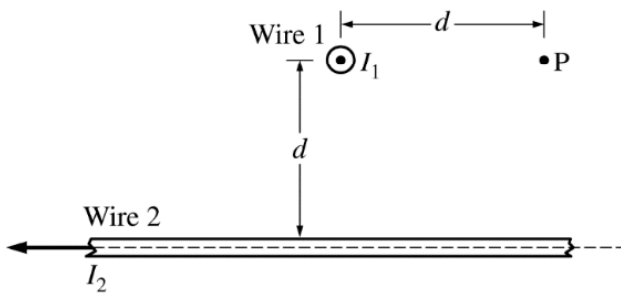


Figure 1. Side view

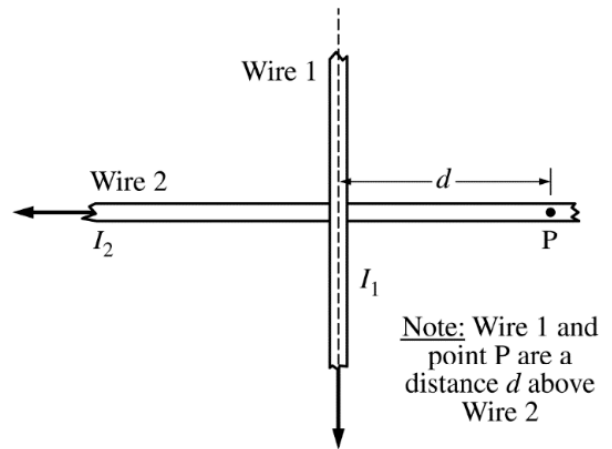


Figure 2. Top view

2. The figures above represent different views of two long, straight, horizontal wires, 1 and 2, carrying currents $I_1 = I$ and $I_2 = 2I$, respectively, in the directions shown. The wires are held in place. In Figure 1, the current in wire 1 is directed out of the page, and wire 1 is a distance d above wire 2. Point P is a horizontal distance d from wire 1 and a distance d directly above wire 2. Express your answers to parts (a) and (b) in terms of I , d , and physical constants, as appropriate.

- Use Ampere's law to derive an expression for the magnitude of the magnetic field at point P due to wire 1.
- Derive an expression for the magnitude of the net magnetic field at point P.
- Calculate the numerical value of the angle to the horizontal for the direction of the net magnetic field at point P.
- Wire 1 is now released. Which of the following best describes the initial motion of wire 1 due to the magnetic field of wire 2? Assume gravitational effects are negligible.
 - Wire 1 will not move.
 - Wire 1 will move upward as viewed in Figure 1.
 - Wire 1 will move downward as viewed in Figure 1.
 - Wire 1 will rotate clockwise as viewed in Figure 2.
 - Wire 1 will rotate counterclockwise as viewed in Figure 2.

Justify your answer.

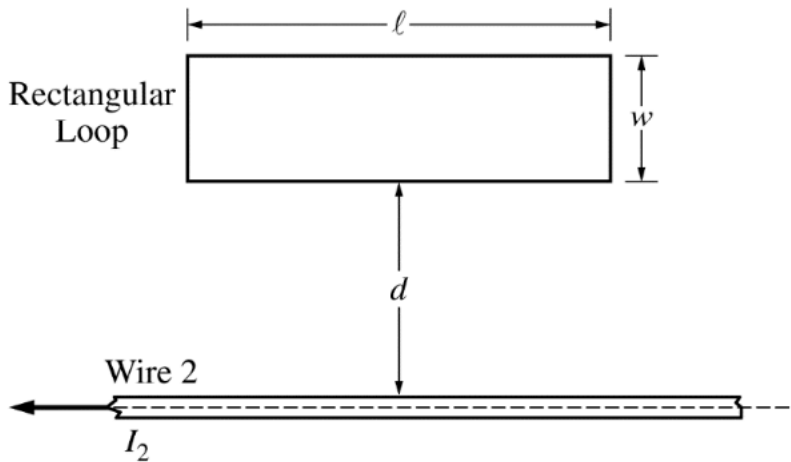


Figure 3. Side view

Wire 1 is now replaced by a conducting rectangular loop of length ℓ , width w , and resistance R . The loop is placed a distance d from wire 2, as shown. The loop, wire, and distance d are all in the plane of the page. The long side of the loop is parallel to the wire. The current I_2 for wire 2 is decreasing linearly as a function of time t according to the equation $I_2 = 2I_0(1 - kt)$, where k is a positive constant with units of s^{-1} .

(e) Of the following, select the integration that will give an expression for the flux Φ as a function of time t .

___ $\Phi = \int_{r=d}^{r=d+w} \frac{\mu_0(2I_0)(1-kt)\ell w}{2\pi} dr$

___ $\Phi = \int_{r=d}^{r=w} \frac{\mu_0(2I_0)(1-kt)\ell w}{2\pi} dr$

___ $\Phi = \int_{r=d}^{r=d+w} \frac{\mu_0(2I_0)(1-kt)}{2\pi r} \ell dr$

___ $\Phi = \int_{r=d}^{r=w} \frac{\mu_0(2I_0)(1-kt)}{2\pi r} \ell dr$

(f) Given that the flux through the rectangular loop as a function of time t is given by the equation $\Phi = \frac{\mu_0 I_0 \ell (1-kt)}{\pi} \ln\left(\frac{d+w}{d}\right)$, derive an expression for the magnitude of the current, if any, induced in the loop. Express your answers in terms of I_0 , d , r , R , w , k , ℓ , and physical constants, as appropriate.

(g) What is the direction of the current, if any, induced in the loop as seen in Figure 3 ?

___ Clockwise ___ Counterclockwise

___ Undefined, because there is no current induced in the loop

Justify your answer.